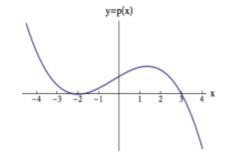
GROUPWORK II

The following problems are taken from a *precalculus final exam* at the University of Michigan.

Problem 1

- **a**. [4 points] The graph of a polynomial p(x) is shown below. The following facts are known about p(x):
 - i) The only zeros of p(x) are x = -2 and x = 3.
 - ii) The degree of p(x) is at most four.
 - iii) The point (1,9) is on the graph of p(x).

Find a formula for p(x).



$$p(x) =$$
_____.

b. [5 points] Let

$$R(x) = \frac{(x^2 + 9)(10x + 1)}{7x^3 - x}.$$

Find all the intercepts and all horizontal and vertical asymptotes of the graph y = R(x). If appropriate, write "None" in the answer blank provided. Your answers should be in **exact form**.

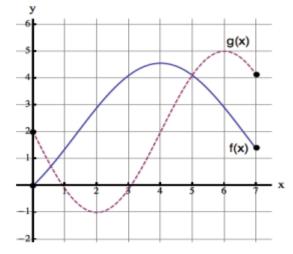
i) x-intercept(s): _____

ii) y-intercept(s): _____

- iii) vertical asymptote(s): _____
- iv) horizontal asymptote(s): _____
- c. [3 points] A law of physics states that the force F (in Newtons) exerted between two objects is inversely proportional to the square of the distance r (in meters) between them, and F = 30 when r = 7. Find a formula for F in terms of r.

Problem 2

3. [8 points] The graphs of the functions f(x) and g(x) are shown below. The domain of f(x) and g(x) is $0 \le x \le 7$.



- a. [4 points]
 - i) Find the range of g(x). Use interval notation or inequalities in your answer.

Answer: _____

ii) For which values of 0 ≤ x ≤ 7 is the function g(x) concave down? Use interval notation or inequalities in your answer.

Answer: _____

iii) For which values of 0 ≤ x ≤ 7 is the function g(x) increasing? Use interval notation or inequalities in your answer.

Answer: _____

b. [4 points] Define the functions:

$$D(x) = g(x) - f(x)$$
 and $R(x) = \frac{g(x)}{f(x)}$.

 For which values of 0 ≤ x ≤ 7 is the function D(x) negative? Use interval notation or inequalities in your answer.

Answer: _____

ii) Find the domain of the function R(x). Use interval notation or inequalities in your answer.

Answer: _____

Problem 3

[11 points] A package is thrown from an airplane. The height of the package (in meters) above the ground t seconds after it was thrown from the airplane is given by the function

$$H(t) = -5t^2 - 10t + 160.$$

a. [2 points] What is the height of the airplane at the time in which the package is thrown? Include units.

Height=_____

b. [3 points] How many seconds does it take for the package to be 10 meters above the ground? Find your answer algebraically. Show all your work.

Answer:

c. [2 points] What is the range of the function y = H(t) in the context of this problem? Give your answer using either interval notation or inequalities.

Answer:

d. [4 points] Another package is released from an airplane at a higher altitude. In this case, the downward velocity V(t) (in meters per second) of the package t seconds after it was released is given by the function

$$V(t) = 50 - 50e^{-0.2t}$$

How long does it take for the package to have a downward velocity of 30 meters per second? Find your answer algebraically. Show all your work step by step. Your answer must be in **exact form**.