

# DISCUSSION QUESTIONS: 21 SEPT

## SHORTCUTS



"Don't worry... I know a short cut."

I Using the short cuts of differentiation *when appropriate*, compute the derivative of each of the following functions.

(A)  $y = 2017 + 3x - \pi x^4 + e^4$

(B)  $y = x \sin x$

(C)  $y = \frac{x+3}{x+7}$

(D)  $y = \frac{x}{\sin x}$

(E)  $y = \frac{\cos x}{x^3 + 9}$

(F)  $y = (x^2 + 4x - 1)(x^3 + 5x^4 - x^3 + x^2 + 3x + 13)$

(G)  $y = \sin^2 x$

(H)  $y = (x^2 + 5x + 1)^2$

- II (a) Find the equations of the *tangent* and *normal lines* to the curve

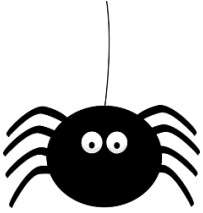
$$y = \frac{x - 4}{x + 1} \text{ at } x = 3.$$

- (b) Find the equations of the *tangent* and *normal lines* to the curve

$$y = \sin x \text{ at } x = \pi/4.$$

- III Using appropriate shortcuts, find formulas for the derivatives of

$$y = \tan x \text{ and } y = \sec x.$$



- IV Charlotte, the spider, dances along the x-axis according to the rule

$$x(t) = t^3 - 3t + 5. \text{ (Here time is measured in } \textit{seconds} \text{ and distance in } \textit{cm}.)$$

- (a) Find Charlotte's *velocity* at time  $t = 2$  sec.

- (b) Find Charlotte's *acceleration* at time  $t = 2$  sec.

- V Sketch the curve  $y = x^2(x - 2)^2$ . Over which interval(s) is the graph *rising*? *falling*? Locate any local maxima or minima.

- VI Sketch the curve  $y = \frac{x-4}{x+1}$  (cf. problem II a). Over which interval(s) is the graph *rising*? *falling*? Locate any *local maxima* or *minima*.

- VII Sketch the curve  $y = xe^x$ . Over which interval(s) is the graph *rising*? *falling*? Locate any local maxima or minima.

- VIII Sketch the curve  $y = \frac{x-3}{x^2+1}$ . Over which interval(s) is the graph *rising*? *falling*? Locate any local maxima or minima.

- IX Consider the curve  $y = b + c \sin x$ . For each of the following values of  $b$  and  $c$ , determine when the graph is rising and when it is falling:

(1)  $b = 3, c = 1$

(2)  $b = c = 1$

(3)  $b = 1, c = 2$

- X Sketch the curve  $y = \frac{1}{x} + x^2$  over the interval  $(0, \infty)$ . Over which interval(s) is the graph *rising*? *falling*? Locate any local maxima or minima.

*What Romantic terminology called genius or talent or inspiration is nothing other than finding the right road empirically, following one's nose, taking shortcuts.*

- Italo Calvino (1923 – 1985)