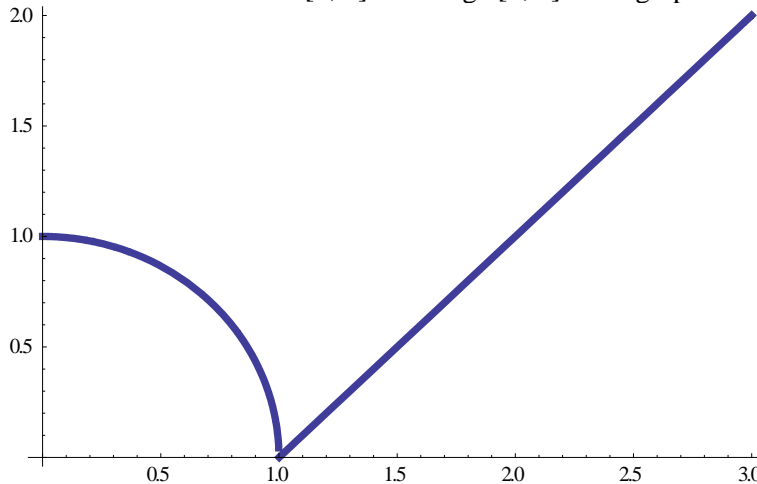


MATH 161: WRITTEN HW A

Due: Wednesday, 5 Sept

Instructions: Write neatly, clearly, and logically. If you work with others, you must hand in your version of the solutions. Also, acknowledge at the beginning of the assignment the people who worked with you or helped you. Also, include any websites that you have consulted.

1. Let $G(x)$ be a function with domain $[0, 3]$ and range $[0, 2]$. The graph of G is displayed below.



Let $A(x) = G(x - 5)$; $B(x) = G(2x)$; $C(x) = 3G(3x) + 1$; and $R(x) = -3G(-x/2)$.

For each of the four functions, A, B, C, R, answer the following three questions.

- Find the *domain* of this function.
- Find the *range* of this function.
- Sketch the graph of this function. Be sure to indicate the x and y scales on your graph!

2. Albertine has inherited a cabin and a huge forest in southeastern Australia. She learns from her environmentalist friends that there are 1400 wombats remaining in her woods and 300 dingos, a natural predator of the wombat. Albertine is distressed to learn that the wombat population is declining by 1.3% per month while the dingo population is growing by 2.4% per month. *When* will the dingo population be *twice* that of the wombat population?



3. The Fifth-Thirty-Second Bank of GammaVille offers 4.1% interest per year *compounded weekly*. How much should Albertine deposit in such a savings account for her to have a balance of \$ 75,000 after twenty years?



4. The number of hemlock trees in the southern Appalachian Mountains is declining because of an infestation of hemlock woolly adelgids (a kind of insect).
- There are $H(d)$ *healthy* hemlock trees in the southern Appalachian Mountains d days after January 1, 2017.
 - There are $I(d)$ infested hemlock trees in the southern Appalachian Mountains d days after January 1, 2017.

Note that all hemlock trees are considered healthy unless they are infested.

- (a) Let $J(w)$ be the number of *healthy* hemlock trees in the southern Appalachian Mountains w weeks after January 1, 2017. Find a formula for $J(w)$ in terms of any or all of the functions H and I .
- (b) Let $F(d)$ be the fraction of the hemlock trees in the southern Appalachian Mountains that are infested d days after January 1, 2017. Find a formula for $F(d)$ in terms of any or all of the functions H and I .
- (c) Let $K(d)$ be the total number of hemlock trees in the southern Appalachian Mountains, in thousands, d days after January 1, 2017. Find a formula for $K(d)$ in terms of any or all of the functions H and I .
- (d) The number of hemlock trees I that are infested in the southern Appalachian Mountains is inversely proportional to the cube of the total amount of money M (in millions of dollars) that the government spends combating the spread of the adelgids. Write a formula for I in terms of M , assuming that there were 2,000 infested trees when the government had spent 3 million dollars.
- (e) The number of hemlock woolly adelgids A (in millions) is also a function of the amount of money M (in millions of dollars) that the government spends to try to preserve the hemlock trees and is given by:

$$A(M) = \frac{4}{M} \quad \text{for } M \geq 4.$$

Find the equation of the horizontal asymptote of $y = A(M)$, and interpret this horizontal asymptote in *practical terms*.

