## WORKSHEET III

## DISKS AND WASHERS



- 1. Find the volume of the solid of revolution obtained by rotating the region bounded by  $y = x^2$ , y = 0, x = 2 about the y-axis.
- 2. Find the volume of the solid of revolution obtained by rotating the region bounded by  $y = \sec x$ , y = 0,  $x = -\pi/4$ ,  $x = \pi/4$ , about the x-axis.
- 3. Find the volume of the solid of revolution obtained by rotating the region bounded by y = x, y = 1, x = 0, about the x-axis.
- 4. Find the volume of the solid of revolution obtained by rotating the region bounded by  $4 x^2$ , y = 2 x, about the x-axis.
- 5. Find the volume of the solid of revolution obtained by rotating the region enclosed by the triangle with vertices (1, 0), (2, 1), and (1, 1), about the y-axis.

- 6. Find the volume of the solid of revolution obtained by rotating the region in the first quadrant bounded above by y = x<sup>2</sup>, below by the x-axis, and on the right by the line x = 1, about the line x = -1.
- 7. Find the volume of the solid of revolution obtained by rotating the region in the second quadrant bounded above by the curve y = x<sup>3</sup>, below by the x-axis, and on the left by the line x = -1, about the line x = -2.

## SHELLS



- 1. Find the volume of the solid obtained by rotating about the the y-axis the region bounded by  $y = 2x^2 x^3$  and y = 0.
- 2. Find the volume of the solid obtained by rotating about the yaxis the region between y = x and  $y = x^2$ .
- 3. Use shells to find the volume of the solid obtained by rotating about the x-axis the region under the curve  $y = x^{1/2}$  from 0 to 1.

- 4. Find the volume of the solid obtained by rotating the region bounded by  $y = x - x^2$  and y = 0 about the line x = 2.
- 5. Find the volume of the solid obtained by rotating the region bounded  $x = 1 + (y - 2)^2$  and x = 2 about the x-axis.
- 6. Find the volume of the solid obtained by rotating the region bounded by  $y = 4x - x^2$  and y = 3 about the axis x = 1.
- Each of following integrals represents the volume of a solid. Describe the solid:

(a) 
$$\int_{0}^{3} 2\pi x^{5} dx$$
  
(b)  $\int_{0}^{1} 2\pi (3-y)(1-y^{2}) dy$   
(c)  $2\pi \int_{0}^{2} \frac{y}{1+y^{2}} dy$ 



COURSE HOME PAGEDEPARTMENT HOME PAGELOYOLA HOME PAGE