**Mathematica Lab III**

Sequences

*(Lab report due: 22 April 2016)*

 **(A)  Graphing sequences**

1. Using the *ListPlot* command in Mathematica, plot the ordered pairs (n, an) for the first 100 terms of each of the seven sequences below. Based upon this evidence, can you guess whether the sequence converges or diverges? In the former case, try to *estimate* the limit of the sequence. Then find the *exact value* of the limit using the *Limit* command.

(a) 

(b) 

(c) 

(d)  *Note:* Here you will need to examine *at least* a few thousand terms.

(e) 

(f) 

(g) 

2. (a) It is a well-known and important fact that the sequence  converges to er. By letting r = 1, ln 2, and ln 3, support this result using Mathematica.

(b) Investigate the behavior of the two related sequences  and . Discuss how the sequences differ in their behavior as *n* grows large. What do you think accounts for these differences?

3. Investigate the behavior of the sequence . Using [Stirling’s formula](https://en.wikipedia.org/wiki/Stirling%27s_approximation), find a simpler expression that approximates this sequence.

**(B)** **Recursively defined sequences**

Using RecurrenceTable, ListPlot and the Nest command, analyze each of the following sequences and find the limit if it exists.

1. c1 = 2, and cn = (cn-1 + 3/cn-1)/2 for n > 2.
2. c1 = 2, and cn = (cn-1 + 5/cn-1)/2 for n > 2.
3. x1 = 1 and xn = xn-1 + cos(xn-1) for n > 2. Can you find the exact value of this limit without employing Mathematica?
4. y1 = 5 and yn = 4/(3 + 2yn-1) for n > 2.
5. z1 = 4 and zn = cos(zn-1) for n > 2.
6. q1 = 3, qn = 2 + 1/sin(qn-1) for n > 2.

**Recursive fish** by Dan Goodman, Math Dept, University of Warwick

 [Course Home Page](http://www.math.luc.edu/~ajs/courses/162spring2016/index.pdf)          [Department Home Page](http://www.math.luc.edu/)        [Loyola Home Page](http://www.luc.edu/)