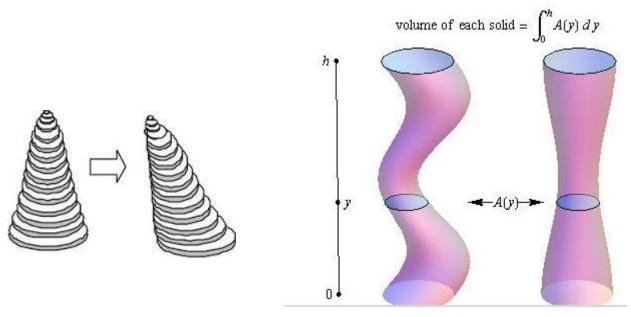
WORKSHEET II

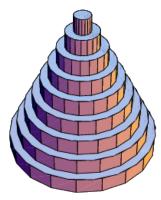
VOLUME & CAVALIERI'S PRINCIPLE



1. The base of a solid is the 2-dimensional region bounded by the curve $y = (\sin x)^{1/2}$ and the interval $[0, \pi]$ on the x-axis. The cross sections perpendicular to the x-axis are equilateral triangles with bases running from the x-axis to the curve. Find the volume of this solid.

2. The cross sections of a solid are squares perpendicular to the x-axis with their centers on the axis. If the square cut off at *x* has edge length of $2x^2$, find the volume of the solid between x = 0 and x = a.

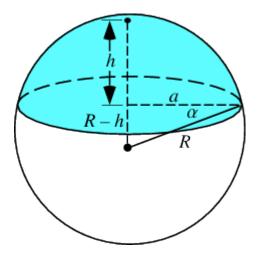
3. Find the volume of a right circular cone of height *h* and base radius *r*. (*Hint:* Revolve an appropriate triangle about the x or y-axis.)



4. Consider the triangle *T* with vertices (0, 0), (2, 0), and (1, 1). Find the volume of the solid of revolution obtained by rotating *T* about:

- (a) the x-axis
- (b) the y-axis
- (c) the vertical line x = 3
- (d) the horizontal line y = -1
- (e) The horizontal line y = 2

5. Consider the portion of the ball of radius *R* centered at the origin for $y \ge R - h$ where 0 < h < R. Find the volume of this *spherical cap*.



6. Consider the region R bounded by the curves $y = x^2$ and y = 2 - x. Find the volume of the solid obtained by rotating R about axis x = -3.

7. Let **C** be the region bounded by the lines y = x, y = 2x and y = 2. Find the volume of the solid obtained by rotating C about the x-axis.

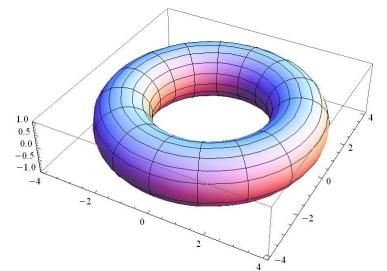
8. Consider the region **A** bounded by the curve $y = x^2 - x^3$ and the x-axis. Find the volume obtained by rotating **A** about:

- (a) the y-axis
- (b) the vertical line x = 1
- (c) the vertical line x = 3
- (d) the vertical line x = -3

9. The region in the xy-plane defined by the inequalities $0 \le x \le 2$ and $x^2/4 \le y \le 1$ is rotated about the given axis below. Find the volume of the solid of revolution so generated.

- (a) the x-axis; (b) the y-axis; (c) the vertical line x = 2;
- (d) the horizontal line y = 1

10. Find the volume of the *torus* obtained by revolving the disk $x^2 + y^2 \le a^2$ about the line x = b, where b > a.





Bonaventura Francesco Cavalieri (1598 – 1647)

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