

1. Define: even number; odd number

2. Prove that if n is odd then so is n^2 .

3. Consider the expression $n^2 + n - 5$, where n is an integer. Compute its values for $n = 1, 2, 3, 4, 5$. Can you make a conjecture? Can you prove your conjecture?

4. Can you *guess* a formula for $1 + 2 + 3 + \dots + n$, where n is a positive integer. Explain how you arrived at this guess.

5. Consider the following problem:
Into how many regions do n lines divide the plane? (Here n is a non-negative integer.)
 - (a) Why is this question ambiguous?

 - (b) Modify this statement so that it is unambiguous.

(c) What is the answer when $n = 1$? $n = 2$? $n = 3$?

(d) What about $n = 4$?

(e) Try $n = 5$.

(f) What is your guess for $n = 6$? Can you discern a pattern?

(g) Analyzing this pattern, can you find a general formula?

6. Carefully state the Product Principle for two finite sets.

7. Carefully state the Addition Principle for two finite sets. (Be careful here.)