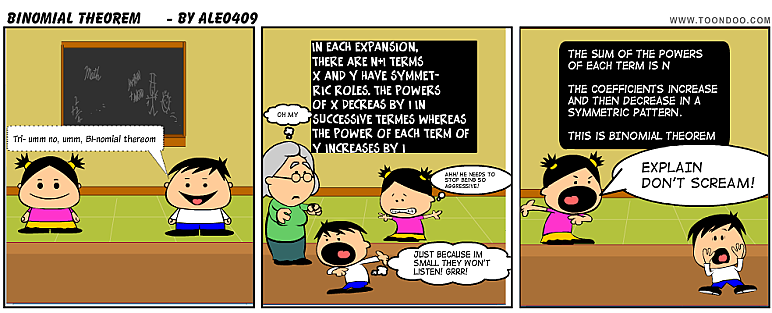
Math 351: Questions for discussion, 5 September 2018



Questions revisited from last week.

1. Define . State some interesting identities.
2. Prove that the sequence Hint: Begin with (1+b)2 > 1+2b for b ≠ 0. Then raise each side to the power 2n.
3. State the binomial theorem for (1 + x)n where *n* is a positive integer.

Prove the binomial theorem using induction. Also, give a combinatorial argument for the binomial theorem. Prove that the sequence is bounded above. Can we conclude that the sequence converges? Why?

1. Define **Euler’s number**, Prove the existence of Euler’s number.



1. What does n>>1 mean? Prove that if {an} and {bn} are increasing sequences for n>>1, then {an + bn} is increasing for n>>1.
2. What is an **Equivalence Relation** on a set X?

**Review exercises on equivalence relations:**

Let R be a relation on a set S. What does it mean for R to be *Reflexive*? *Symmetric*? T*ransitive*? What is an *equivalence relation* on S? Explain how an equivalence relation corresponds to a partition on the set S. What does the term *equivalence class* mean?

1. Determine which of the three properties “reflexive,” “symmetric,” and “transitive,” apply to each of the following relations on the set of integers. For each relation that is an equivalence relation, describe the equivalence classes.

a R b iff

1. a = b
2. a < b
3. a < b
4. a | b
5. |a| = |b|
6. a2 + a = b2 + b
7. a < |b|
8. ab > 0
9. ab > 0
10. a + b > 0
11. a ≡ b mod 4
12. a ≡ b mod m (where m > 0)
13. Do the same as in (A) for the following relations on the set of all people. p R q iff
    1. p “is a father of” q
    2. p “is a sister of” q
    3. p “is a friend of” q
    4. p “is an aunt of” q
    5. p “is a descendant of” q
    6. p “has the same height” as q
    7. p “likes” q
    8. p “knows” q
    9. p “is married to” q

**Exercises for groupwork.**

* 1. Prove that the sequence is monotone.
  2. Let Prove that
  3. Using the Completeness Property of **R**, prove that the sequence converges.
  4. Prove that the sequence … converges. Can you find its limit? Note that this sequence can also be defined recursively, *viz.*