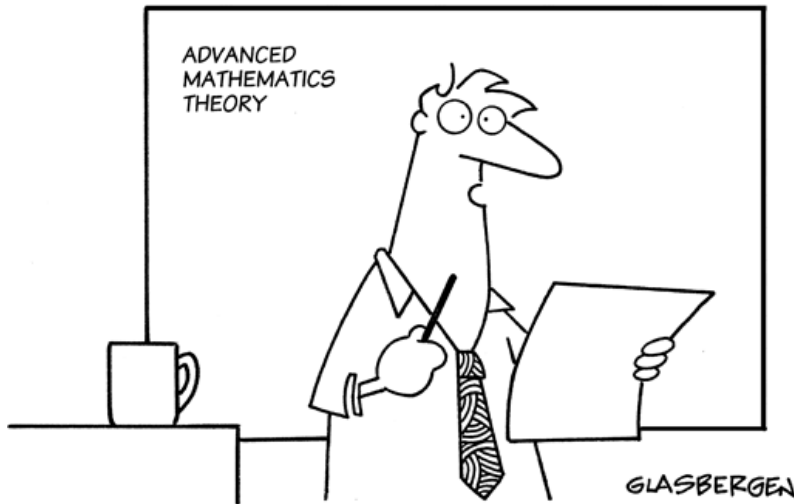


No graphing calculators permitted!

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“Today’s test is 70% of your final grade which makes up 35% of your grade for the semester and 20% of your GPA for 50% of your scholastic career for 15% of the curriculum. If you can explain this to the person next you, you pass the test.”

1. [10 pts] How many real roots does each of the following polynomials possess? List all of the roots. In case there are no real roots, write NONE. (You need not show your work.)

(a) $y = x^4 - 16$ Answer: number of roots = ; the roots are: $x =$

(b) $y = x^2 + 1789$ Answer: number of roots = ; the roots are: $x =$

(c) $y = x^3 - 1$ Answer: number of roots = ; the roots are: $x =$

(d) $y = (x - 9)^{99}(x + 2018)^5(x - 11)x^4$ Answer: number of roots = ; the roots are: $x =$

(e) $y = (x^2 - 81)(x^2 + 7x + 12345)$ Answer: number of roots = ; the roots are: $x =$

2. [10 pts] In this problem, we consider two functions:

➤ $W(s)^*$ is the wind-chill (in degrees Fahrenheit) when the temperature is 30 degrees Fahrenheit and the wind speed is s mph (miles per hour).

➤ $B(c)$ is the time (in minutes) it takes to develop frostbite on exposed skin when the wind-chill is c degrees Fahrenheit.

Assume both W and B are invertible (that is, each function has an inverse).

Fill in each blank below with one of the possible answers given below.

Note that a given answer may be used in more than one blank and that not all possible answers will be used.

Possible Answers:

20	$W(20)$	$B(20)$	$W(20)+B(20)$
$W^{-1}(20)$	$B^{-1}(20)$	$W(B(20))$	$B(W(20))$
$W^{-1}(B^{-1}(20))$	$B^{-1}(W^{-1}(20))$	$W(B^{-1}(20))$	$B(W^{-1}(20))$

Assume throughout this problem that the temperature is 30 degrees Fahrenheit.

- a. If the wind-chill is _____ degrees Fahrenheit, the wind speed is 20 mph.
- b. When the wind-speed is 20 mph, exposed skin will develop frostbite in _____ minutes.
- c. If the wind-chill is 20 degrees Fahrenheit, then the wind speed is _____ mph.
- d. If the wind-chill is 20 degrees Fahrenheit, then it will take exposed skin _____ minutes to develop frostbite.
- e. When the wind-chill is $B^{-1}(20)$ degrees Fahrenheit, exposed skin will develop frostbite in _____ minutes.

* *Wind-chill* is the temperature “it feels like.”

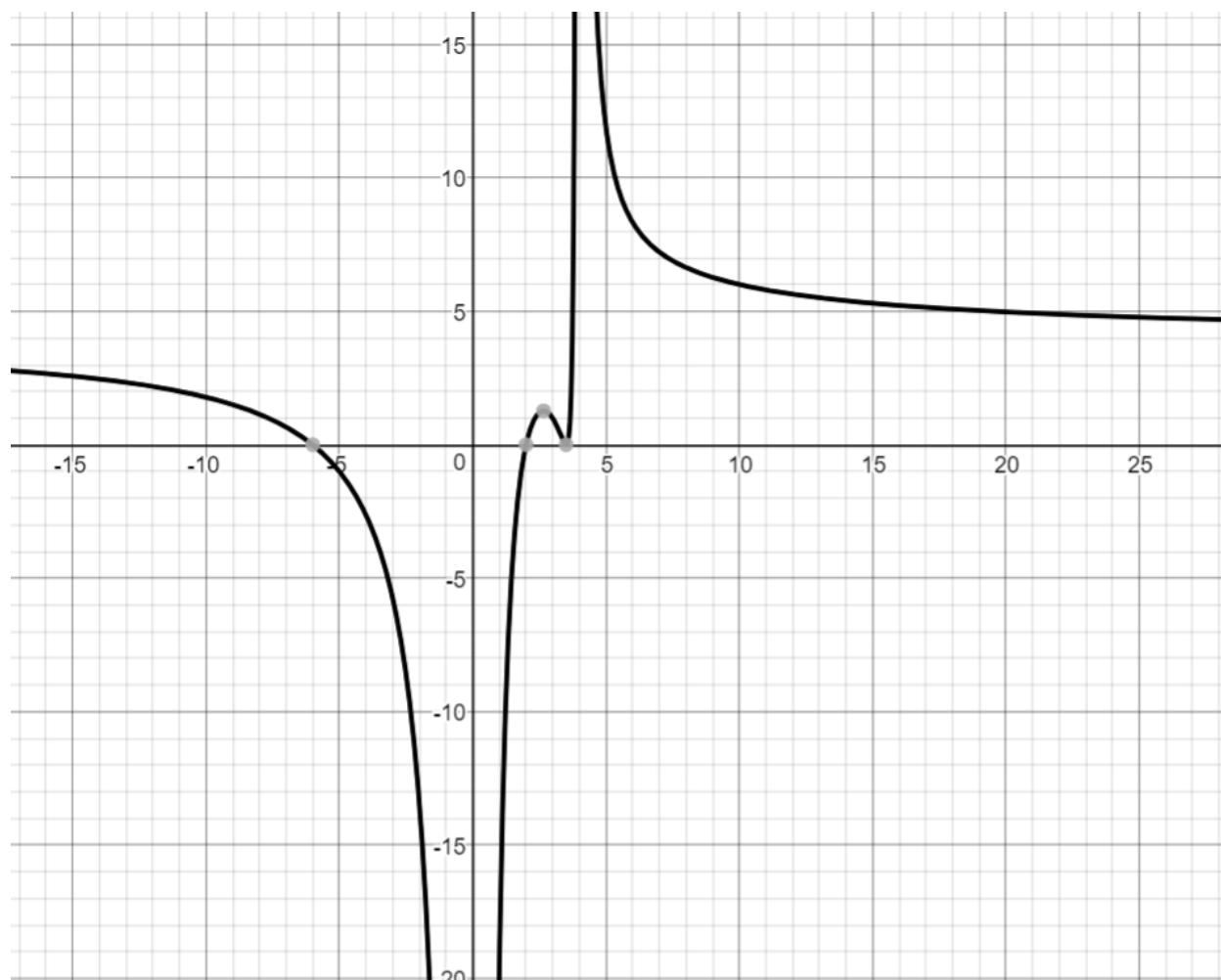
3. [10 pts] Write an equation of a rational function that is represented by the following graph. (Note: there are many possible correct answers.)

Assume that

Zeros: 2, $7/2$, -6

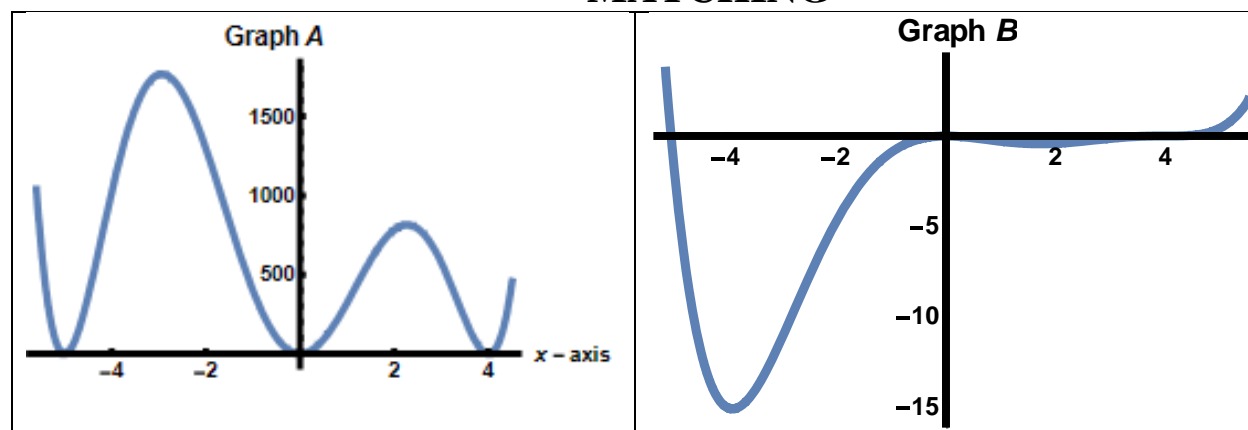
Singularities: $x = 0$, $x = 4$

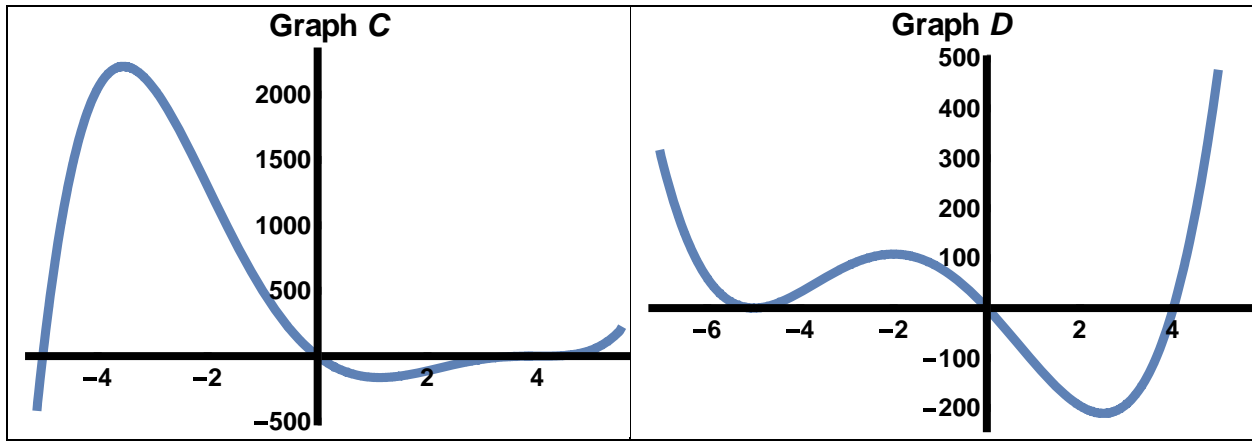
Limiting behavior: $y \rightarrow 4$ as $x \rightarrow \pm\infty$



4. [8 pts]

MATCHING





➤ Enter your answers here:

$f(x) = x^2(x - 4)^3(x + 5)$ corresponds to Graph _____

$f(x) = x^2(x - 4)^2(x + 5)^2$ corresponds to Graph _____

$f(x) = x(x - 4)(x + 5)^2$ corresponds to Graph _____

$f(x) = x(x - 4)^3(x + 5)$ corresponds to Graph _____

Extra Credit Riddle: [7 pts] On the island of Oz, each of the residents is either a knight or a knave. Knights *always* tell the *truth*; Knaves *always* lie. Two residents of the island, Albertine and Beatrice, are approached by a reporter for Loyola's Phoenix. Albertine says "We are the same kind.", but Beatrice says "We are of different kinds." What, if anything, can the reporter conclude? Explain!