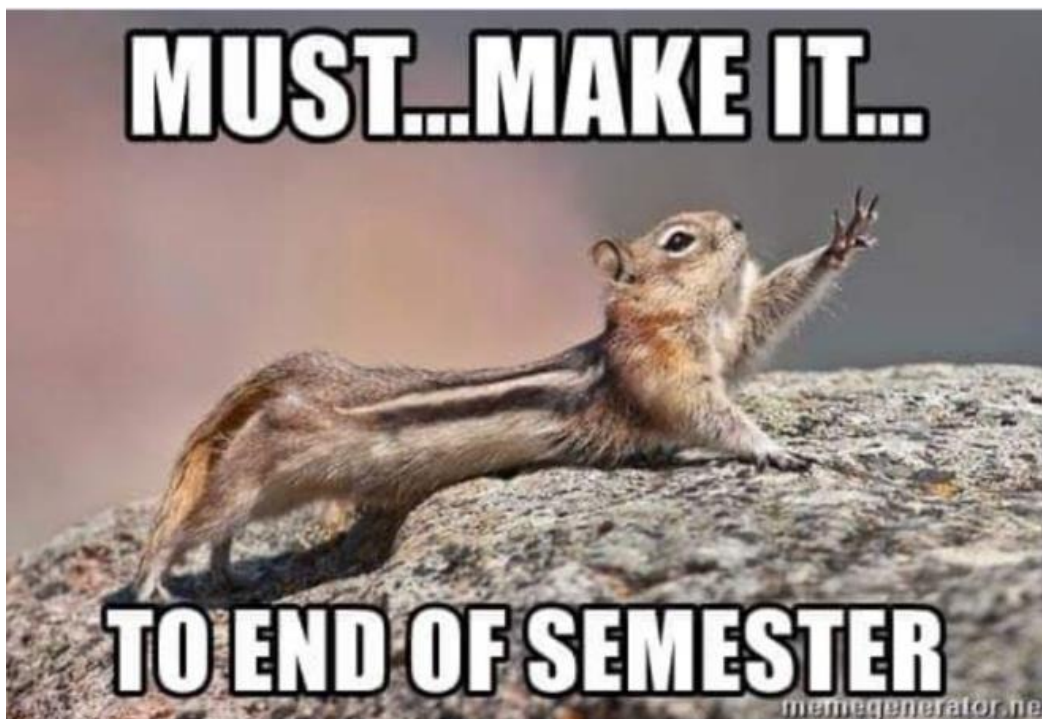


## REVIEW SHEET FOR FINAL EXAM: MATH 161



*Study: Chapters 1 – 5 and section 6.1 (excluding section 2.4 and 4.8) of Stewart.*

### 1. Understanding graphs

- A. precalculus strategy (domain, zeroes, singularities, sign analysis, limiting behavior, symmetry)
- B. regions of increase and decrease (first derivative test for local extrema)
- C. concavity and points of inflection
- D. second derivative test for local extrema
- E. Graphing functions of the form  $g(x) = \int_a^x f(t)dt$
- F. geometric differentiation
- G. geometric anti-differentiating

### 2. Differential Calculus

- A. limit definition of the derivative
- B. finding tangent and normal lines
- C. continuity
- D. differentiation rules including sum, product, and quotient

- E. chain rule
- F. meaning of the derivative as a rate of change
- G. higher-order derivatives
- H. l'Hôpital's rule
- I. linearization: estimating numerical values using a tangent line
- J. related rate problems
- K. optimization problems

### 3. Definition and meaning of the definite (Riemann) integral.

- A. area between curves
- B. distance, velocity, acceleration problems
- C. limit of a Riemann sum equals a definite integral
- D. average value of a function
- E. properties of the indefinite and the definite integral
- F. Fundamental Theorem of Calculus! (*both versions*)
- G. net change theorem
- H. Leibniz's extension of FTC for differentiation of an integral
- I. implicit and logarithmic differentiation
- J. differential equations; initial value problems

### 4. Techniques of integration

- A. judicious guessing
- B. substitution (for both indefinite and definite integrals) *aka* change of variable theorem
- C. use of symmetry in evaluating definite integrals (odd functions, even functions)
- D. verifying an integration formula employing differentiation

### 5. Logs and exponential functions

- A. log and exp as inverse functions of one another
- B. properties of logs and exponentials:  $\log(ab)$ ,  $\log(a/b)$ ,  $\log(a^p)$ ,  $\exp(a + b)$ , etc.; change of base formula for logs
- C. differentiating and integrating a function of the form  $b^x$
- D. differentiating functions of the form  $f(x)^{g(x)}$

### 6. Statements of Theorems

- A. Sandwich (*aka* Squeeze) Theorem

- B. limit as  $\theta \rightarrow 0$  of  $\frac{\sin \theta}{\theta}$
- C. Intermediate Value Theorem
- D. Extreme Value Theorem
- E. Rolle's Theorem
- F. Mean Value Theorem and its Corollaries
- G. Fundamental Theorem of Calculus (*both versions*)
- H. Net Change Theorem

*Examinations are formidable even to the best prepared, for the greatest fool may ask more than the wisest man can answer.*

- C. C. Colton, **Lacon**



Henri Rousseau. **Exotic Landscape**. (1910)