

Name (print): \_\_\_\_\_ Signature: \_\_\_\_\_

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You have 30 minutes. Show your work. Notes not allowed! Problems are on both sides of this sheet.

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**Problem 1.** (6 pts) Consider the function  $7 - 4 \sin(13x)$ .

a. What is its range?

*Solution:*  $[7 - 4, 7 + 4]$ , hence  $[3, 11]$ .

b. What is its period?

*Solution:*  $\frac{2\pi}{13}$ .

**Problem 2.** (5 pts) For the functions  $f(x) = 3 \sin(x^2)$  and  $g(x) = 5e^x$ , find the following:

a.  $g(f(0)) =$

*Solution:*  $f(0) = 0$ ,  $g(f(0)) = g(0) = 5e^0 = 5$

b.  $f(g(x)) =$

*Solution:*  $f(g(x)) = f(5e^x) = 3 \sin((5e^x)^2)$ .

c.  $\ln(2g(x)) - x =$  *Simplify the answer to c.!*

*Solution:*  $\ln(2g(x)) - x = \ln(10e^x) - x = \ln 10 + \ln e^x - x = \ln 10 + x - x = \ln 10$ .

**Problem 3.** (5 pts) The half-life of a certain radioactive substance is 12 hours. There are 8 grams present initially.

a. Express the amount of substance remaining as a function of time  $t$ .

b. When will there be 1 gram remaining?

**Problem 4.** (4 pts) If the domain of  $f : \mathbb{R} \rightarrow \mathbb{R}$  is  $[0, \infty)$  and  $g(x) = x^2 + x - 6$ , find the domain of  $f(g(x))$ .

*Solution: domain of  $f$  is  $[0, \infty)$ , hence for  $f(g(x))$  to make sense, we must have  $g(x) \geq 0$ . So  $x^2 + x - 6 \geq 0$ , which means  $x \leq -3$  or  $x \geq 2$ . Said differently, the domain of  $f(g(x))$  is  $(-\infty, -3]$  and  $[2, \infty)$ .*