

Name (print): \_\_\_\_\_ Signature: \_\_\_\_\_

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You have 30 minutes. Show your work. Notes not allowed! Problems are on both sides of this sheet.

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**Problem 1.** (8 pts) Use truth tables to show the following:

$P \text{ AND } (Q \text{ OR } R)$  is equivalent to  $(P \text{ AND } Q) \text{ OR } (P \text{ AND } R)$

**Problem 2.** (6 pts) Consider the following statement:

$$\text{If } x \geq 0 \text{ and } y \geq 0 \text{ then } xy \geq 0.$$

Do the following:

**a.** Write the contrapositive statement and determine whether it is true or not.

**b.** Write the converse statement and determine whether it is true or not.

**Problem 3.** (6 pts) Prove or disprove the following statement:

$$x \in \{y \in \mathbb{R} \mid y^2 - 3y \leq 0\} \implies 0 \leq x \leq 5.$$