

Name (print): \_\_\_\_\_ Signature: \_\_\_\_\_

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You have 30 minutes. Show your work. Notes not allowed! Problems are on both sides of this sheet.

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**Problem 1.** Is the number  $3.2457457457457\dots$  rational or not? If yes, write it as a fraction. If not, give reasons.

**Problem 2.** Prove that  $\sqrt[4]{6}$  is not a rational number.

**Problem 3.** Write down an explicit formula for a bijection from  $\mathbb{Z}$  to  $\mathbb{N}$ .

**Problem 4.** Suppose that the coefficients  $a, b, c$  of the quadratic equation  $ax^2 + bx + c = 0$  are rational and that the equation has two distinct solutions. How many of these solutions can be rational? Give all necessary examples and proofs.